

- e) The results observed in a), valid for any trigonometric point in the 1st quadrant, are generalized and bring us to the definition of the Cartesian coordinates of any trigonometric point $P(t)$.

We have: $P(t) = (\cos t, \sin t)$ where $0 \leq t \leq 2\pi$.

Calculate, using a calculator, the Cartesian coordinates of

1. $P(100^\circ)$ $(-0.17, 0.98)$ 2. $P(200^\circ)$ $(-0.94, -0.34)$ 3. $P(300^\circ)$ $(0.5, -0.87)$

CARTESIAN COORDINATES OF A TRIGONOMETRIC POINT

- Given a trigonometric point $P(t)$. ($0 \leq t \leq 2\pi$)
 - the x -coordinate of $P(t)$ is equal to $\cos t$.
 - the y -coordinate of $P(t)$ is equal to $\sin t$.

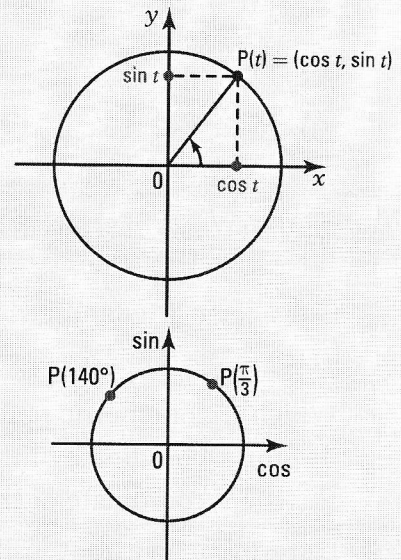
Note that:

$$P(t) = (\cos t, \sin t)$$

By convention, we call the x -axis the **cosine axis**, and the y -axis the **sine axis**.

Ex.: $P\left(\frac{\pi}{3}\right) = \left(\cos \frac{\pi}{3}, \sin \frac{\pi}{3}\right) = \left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$

$P(140^\circ) = (\cos 140^\circ, \sin 140^\circ) = (-0.7660, 0.6428)$



9. For each of the following trigonometric points $P(t)$, indicate
- the quadrant in which the trigonometric point is located.
 - the sign of $\cos t$ and the sign of $\sin t$.

a) $P(160^\circ)$

- II
- $(-, +)$

b) $P(350^\circ)$

- IV
- $(+, -)$

c) $P(-150^\circ)$

- III
- $(-, -)$

d) $P(750^\circ)$

- I
- $(+, +)$

e) $P\left(\frac{5\pi}{6}\right)$

- II
- $(-, +)$

f) $P\left(\frac{5\pi}{3}\right)$

- IV
- $(+, -)$

g) $P\left(-\frac{2\pi}{3}\right)$

- III
- $(-, -)$

h) $P\left(\frac{10\pi}{3}\right)$

- III
- $(-, -)$

10. Using a calculator, determine the coordinates of the following trigonometric points to the nearest thousandth.

a) $P(175^\circ)$ $(-0.996, 0.087)$

b) $P(625^\circ)$ $(-0.087, -0.996)$

c) $P\left(\frac{11\pi}{5}\right)$ $(0.809, 0.588)$

d) $P\left(-\frac{29\pi}{6}\right)$ $(-0.866, -0.5)$

11. Knowing that $P(t) = \left(\frac{3}{5}, \frac{4}{5}\right)$ is a trigonometric point, determine

a) $\cos t = \frac{3}{5}$ b) $\sin t = \frac{4}{5}$ c) $\tan t = \frac{4}{3}$

d) $\sec t = \frac{5}{3}$ e) $\csc t = \frac{5}{4}$ f) $\cotan t = \frac{3}{4}$